TU Delft Faculty of Electrical Engineering, Mathematics, and Computer Science Circuits and Systems Group

ET4350 Applied Convex Optimization

ASSIGNMENT

MIMO Detection

1 Context

Multiple Input Multiple Output (MIMO) detection is a common problem encountered in digital communications. In a MIMO system, several transmit antennas simultaneously send different data streams. The receiver often observes a linear superposition of separately transmitted information symbols. From the receiver's perspective, the problem is then to separate the transmitted symbols. This is basically an inverse problem with a finite-alphabet constraint.

This exercise consists of two parts: (a) formulate the MIMO detection problem as a suitable convex optimization problem; and (b) implement the MIMO receiver. In a group of 2 students, make a short report (4-5 pages; pdf file) containing the required Matlab scripts, plots, and answers. Also, prepare a short presentation to explain your results and defend your choices.

Dataset explanation

Consider a generic N-input M-output model

$$\mathbf{y}_{c} = \mathbf{H}_{c}\mathbf{s}_{c} + \mathbf{v}_{c}.$$

Here, $\mathbf{y}_c \in \mathbb{C}^M$ is the received vector, $\mathbf{H}_c \in \mathbb{C}^{M \times N}$ is the MIMO channel, $\mathbf{s}_c \in \mathbb{C}^N$ is the transmitted symbol vector, and $\mathbf{v}_c \in \mathbb{C}^M$ is an additive white Gaussian noise vector. In this application example we assume that the transmitted symbols follow a quaternary phase-shift-keying (QPSK) constellation; i.e., the entries of \mathbf{s}_c belong to the finite-alphabet set $\{\pm 1 \pm j\}$. The dataset MIMODetection.mat in the course webpage contains the received

data symbols, channel matrix, and the true data symbols. The aim is to detect \mathbf{s}_c from \mathbf{y}_c in the maximum likelihood sense with the assumption that the MIMO channel is known.

2 Assignment

You will have to answer the following questions:

- 1. (2 pts) Formulate the MIMO detection problem as an optimization problem. Suggest a suitable convex approximation (i.e., derive a convex relaxed problem) if the true problem is not convex. Motivate the proposed formulation as well as the relaxation.
- 2. (2 pts) Implement the proposed convex optimization problem in your favorite off-the-shelf solver (e.g., CVX, SeDuMi, or YALMIP). How does this ready-made software solve your problem? Comment on the number of iterations, CPU time, and algorithm the ready-made solver uses.

Optional: Does your solution based on randomized rounding follow Goemans and Williamson's theorem; see the reference.

- 3. (5 pts) Implement a low-complexity algorithm (e.g., projected (sub)gradient descent for the above problem, or provide a first-order algorithm to solve the primal and dual problems). Compare the obtained results with the solutions from the off-the-shelf solver. Comment on the number of iterations, CPU time, and convergence of your low-complexity algorithm.
- 4. (1 pt) Make a short presentation explaining your results clearly in 5 minutes.

3 Reference

Z.-Q. Luo, W.-K. Ma, A. Man-Cho So, Y. Ye, and S. Zhang, "Semidefinite Relaxation of Quadratic Optimization Problems," IEEE Signal Processing Magazine, vol. 27, no. 3, May 2010.

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